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## **Unifying grain shape effects in granular flows down a rough incline**

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## Unifying grain shape effects in granular flows down a rough incline

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### Abstract

Granular materials in nature are nearly always non-spherical, but particle shape effects in granular flow remain largely elusive. Here we use the discrete element method (DEM) to simulate dense granular flows down a rough incline with varying microscopic parameters and particle shapes. For each particle type, we vary the flow thickness  $h$  and slope angle  $\theta$  to extract the  $h_{\text{stop}}(\theta)$  curves (below which flow ceases) and the  $Fr = h/h_{\text{stop}}$  relations following Pouliquen's approach [1], where  $Fr = u/\sqrt{gh}$  is the Froude number,  $u$  is the mean flow velocity, and  $g$  is the gravitational acceleration. For microscopic parameters, we find that the friction coefficient ( $\mu_s$ ) has a significant impact on the flow, saturating at around  $\mu_s = 0.5$ , for spherical and non-spherical particles. Other parameters (particle stiffness with linear and Hertz models, Poisson's ratio, and restitution coefficient) have a minor influence. For non-spherical particles, we first focus on the particle length-to-diameter aspect ratios (AR). The  $Fr-h/h_{\text{stop}}$  curves show an intriguing nonlinear dependence on AR, with two plateaus at small and large AR, respectively [2]. Similar behaviors are observed for other particle shapes (flatness and angularity), indicating that Pouliquen's flow rule is not universal across granular materials. Finally, we show that a recent velocity scaling [3] based on a shear stress argument can collapse data for all flow conditions and particle shapes, including cubes, pyramids, elongated particles, flat particles, and realistic sand-shaped particles, which represents a promising grain-shape-unifying flow rule for granular avalanches.

### References

- [1] Pouliquen O. Scaling laws in granular flows down rough inclined planes. *Physics of Fluids*, 1999, 11(3): 542-548.
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- [3] Wu Y, Pähzt T, Guo Z, Jing L, et al. Unified flow rule of undeveloped and fully developed dense granular flows down rough inclines. *Physical Review Letters*, 2025, 134(2): 028201.