



# SBGf Conference

18-20 NOV | Rio'25

**Sustainable Geophysics at the Service of Society**

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**Submission code: WLAGW580LB**

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## **Comparisons of FWIs with different objective functions**

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This paper was prepared for presentation during the 19<sup>th</sup> International Congress of the Brazilian Geophysical Society held in Rio de Janeiro, Brazil, 18-20 November 2025. Contents of this paper were reviewed by the Technical Committee of the 19<sup>th</sup> International Congress of the Brazilian Geophysical Society and do not necessarily represent any position of the SBGf, its officers or members. Electronic reproduction or storage of any part of this paper for commercial purposes without the written consent of the Brazilian Geophysical Society is prohibited.

### Introduction

Full Waveform Inversion (FWI) has been widely applied in the oil and gas industry, mineral exploration, and geotechnical studies, offering superior spatial resolution for determining the properties that affect the propagation of seismic waves compared to other methods and a better representation of geological characteristics.

The essence of FWI lies in minimizing the difference between the seismic traces calculated from an underground model and the observed seismic waves (real seismic data). For this purpose, objective functions are used to quantify this discrepancy. This function can be minimized through different methods, such as the method of steepest descent, Newton's method and its variants and the conjugate-gradient method. The gradient of the objective function, which is necessary in the methods mentioned, is calculated using the adjoint state method. These methods iteratively adjust the subsurface property model to minimize the objective function.

Different objective functions can be employed, such as the L2 norm, which is the most common and allows for fine-tuning of the model. However, the L2 norm is subject to the cycle skipping problem, which can trap the objective function in a local minimum, thus preventing the progress to a global minimum. To mitigate this issue, the multi-scale approach, regularization techniques and other objective functions have been proposed in the literature. For instance, the multi-scale approach for the frequency starts the inversion with the low frequencies of the data and, step by step, includes the higher frequencies. The multi-scale approach can also be done using offset, layer striping, etc. Regularization uses prior knowledge to guide the inversion towards the desired model. Examples of other objective functions are the adaptive norm, functions that use the envelope or phase of seismic traces, time-lag norm, cross-correlation, etc.

That said, this work aims to compare the robustness of some functionals reported in the specialized literature, evaluating convergence, spatial resolution of the solution and other metrics, as well as the influence of the initial model, which also affects the efficiency of the inversion.

### Method and/or Theory

Investigations for the Marmousi2D geological model are underway with different objective functions using the adjoint method for various initial models. Other synthetic geological models will be tested to determine which is the best objective function or which is the best according to the complexity of the geology faced.

### Conclusions

In summary, Full Waveform Inversion (FWI) represents a significant advancement in seismic processing that could lead to better seismic interpretation, allowing for a more accurate understanding of subsurface characteristics. Objective functions play a central role in this process, guiding the optimization of the model and ensuring that the estimates are both accurate and relevant for practical applications in the exploration and production of natural resources. The continuous evolution of FWI techniques, coupled with increased computational capacity, promises further improvements in the quality and efficiency of seismic inversions.