

# ESTIMATING AND ANALYZING THE STABILITY OF BRAZILIAN GNSS STATIONS FOR TECTONIC STUDIES

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**ABSTRACT.** The detailed study of stresses and strains is fundamental for geophysical and geodetic studies, enabling the development of plate motion models, geodynamic processes and several proposals. GNSS positioning has been used to estimate these stresses and strains. However, for the accuracy required, it is necessary a rigorous assessment of the behavior of GNSS stations and their position time series. This paper aims to analyze the influence of the different types of geodetic monuments present in the Brazilian GNSS Continuous Monitoring Network by estimating and characterizing noise in the time series and investigating variables that can affect the stability of the stations to establish criteria for using this data in tectonic and geodynamic studies. The evaluation of 119 GNSS stations throughout Brazil indicates the significant presence of random walk noise in some of these stations, detected by analyzing the magnitude of the noise and the spectral index. It was found that the stations with unstable monuments have been observed for at least eight years and are mostly in coastal areas or under the influence of large watercourses.

**Keywords:** Time series analysis; Geodetic monuments; Noise characterization; Geodynamic processes

## Introduction

The main components of the stresses acting on the South American Plate are generated by the ongoing subduction of the Nazca Plate and the formation of young crust on the mid-Atlantic ridge (Rocha et al., 2016; Marotta et al., 2015; Lima et al., 2000; Norabuena et al., 1998). Therefore, global stress models characterize the South American intraplate region according to these regional components (Assumpção et al., 2016). However, several studies have indicated the existence of stresses resulting from local rheological and structural features that can either potentially modify both the direction and magnitude

or intensify the field of tectonic stresses, as well as affect significantly the observed deformations (Calais et al., 2006; Agurto-Detzel et al., 2014; Assumpção et al., 2016; Yadav and Tiwari, 2018).

The detailed study of resulting stresses and deformations is fundamental for geophysical and geodetic applications, as it allows modeling the movement of plates and geological blocks, crustal and mantle geodynamics processes while supporting climate change studies and the understanding of associated phenomena and processes (Kierulf et al., 2021).

In Brazil, several studies have raised essential hypotheses and observations regarding the field of stresses. Agurto-Detzel et al. (2014) highlighted the difficulty of characterizing stresses from seismological studies using focal mechanism, due to the low magnitude of intraplate seismic events. Assumpção et al. (2004), Barros et al. (2009), Chimpliganond et al. (2010), and Rocha et al. (2016), among others, point to the crustal and lithospheric thinning of some regions, and the presence of sedimentary basins, pre-existing faults, and other geological factors, as favorable for the concentration of stress.

GNSS positioning of the stations, where a position time series allows estimating motion and deformation rates, has been widely used to improve the estimation and analysis of the mentioned above processes and mechanisms (Marotta *et al.*, 2015; 2013a; 2013b) to assist in the understanding of regional tectonic and geodynamic processes. However, a more rigorous assessment of the behavior of GNSS stations and their position time series is essential to achieve the required accuracy.

To this end, while emphasizing Brazil, this work sought to analyze the influence of the different types of geodetic monuments present in the Brazilian GNSS Continuous Monitoring Network by estimating and characterizing the noise in the time series while investigating the variables that may affect the stability of GNSS stations, as to establish criteria for using these data in tectonic and geodynamic studies.

It is noteworthy that, for the most part, RBMC stations were not designed for geotectonic studies, and it is essential to develop a strategy to identify stations whose levels of instability are incompatible with the desired application since surface processes also affect the GNSS time series and propagate to the velocity and deformation estimates.

Thus, the horizontal velocities for each of the GNSS stations were also estimated in this study in addition to the proposed analysis. These velocities allow dynamic monitoring of reference frames, evaluation of movements caused by seismic events, estimation of

movements between tectonic plates and several other applications in geodesy (Sánchez and Drewes, 2020).

## 1. Noise in time series of GNSS solutions

The use of the GNSS position time series for estimating a model that describes the motion of a geological plate or block requires that these series record both the phenomenon of interest and other phenomena. Therefore, defining a functional model that expresses the present phenomena and allows their differentiation should be considered.

Currently, Nikolaidis (2002), Cenni *et al.* (2012), and Farolfi and Ventisette (2015) have presented a well-accepted functional model (Equation 1) that considers the aforementioned phenomena:

$$y(t_i) = a + b(t_i - t_0) + \sum_{k=1}^2 c_k \sin(2\pi k t_i + \varphi_k) + \sum_{j=1}^J d_j H(t_j - t_i) + v_i \quad (1)$$

where  $y(t_i)$  represents the position observed at the point for each direction ( $n, e, u$ ), at the time  $t_i$ ;  $a$  is the position at a time  $t_0$ ;  $b$  is the speed for each direction ( $n, e, u$ ),  $c_k$  are the annual and semi-annual amplitudes;  $\varphi_k$  are the phases;  $d_j$  is the discontinuity introduced at the time  $t_j$ ;  $H$  is the jump function, with  $H(t_j - t_i) = 0$  if  $t_i < t_j$  and  $H(t_j - t_i) = 1$  if and  $H(t_j - t_i) = 1$  if  $t_i \geq t_j$ ; and  $v_i$  is the residue.

The model represented in Equation 1 can be estimated deterministically. However, since the residuals ( $v$ ) can represent both unmodeled effects and errors associated with observations, they can affect the estimation of unknown parameters and their uncertainties. Therefore, if the GNSS coordinate solutions are strongly correlated in time (Amagua *et al.*, 2018), using a stochastic method to estimate more realistic uncertainties of the parameters estimated using the observed data.

In general, the estimated residuals can be considered stochastic noise and may be described either by a Power Law process (Mandelbrot, 1983; Agnew, 1992; Williams *et al.*, 2004) or the behavior in the time domain expressed as:

$$P_y = P_0 \left( \frac{f}{f_0} \right)^k \quad (2)$$

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where:  $f$  is temporal frequency,  $P_0$  and  $f_0$  are the normalization constants and  $k$  is the spectral index, whose values vary in the interval  $[-3, 1]$ .

In Equation 2, noise levels can be analyzed regarding the index  $k$ , which allows for classifying the station noise according to the presence of fractional Brownian movement, in the interval  $-3 < k < -1$ , and fractional Gaussian noise for  $-1 < k < 1$ , so that  $k = 0$  indicates classic white noise,  $k = -1$  indicates fractal noise, or flicker; and  $k = -2$  indicates random walk noise (Williams *et al.*, 2004).

While white noise is associated with errors in observations and characteristics of the GNSS receiver hardware, flicker noise is associated with multipath (Dmitrieva *et al.*, 2016) and a wide variety of dynamic processes, including the Earth's oscillation around its axis and uncertainties in the time measured by satellites and receivers, in addition to atmospheric effects (Williams *et al.*, 2004).

Also, according to Williams *et al.* (2004), the random walk noise is mainly associated with the instability of the geodetic monument due to the changing conditions at the placement site, whether placed on soil, rock, building roofs, etc. In this same study, the authors analyzed eight different types of geodetic monuments, from those anchored in the basement to those installed on concrete slabs on the roof and directly on the ground, and reported that stations installed on concrete pillars on the ground only performed better than stations installed on oil platforms, which are susceptible to a wide variety of movements.

It is observed that random walk is a type of non-stationary noise and; thus, its characterization does not allow future prediction, its detection in time series depends on the amount of data, sampling frequency, and amplitudes relative to other types of noise, among other factors. Also, the instability of the geodetic monument can be minimized using carefully designed structures anchored in a rocky basement, decoupled from the surface, and counterbalanced regarding the winds (Wyatt, 1989; Bock *et al.*, 1997).

Despite the above, the RBMC stations are mostly located on concrete roofs of public buildings and concrete pillars in the ground (Table 1), prioritizing longevity, security, and the infrastructure (electricity and internet) necessary for the uninterrupted operation of the equipment. Amagua *et al.* (2018) and Ramos *et al.* (2022) reported that, compared to the other types of noise, the RBMC stations have significant white noise levels, while the white noise and flicker combination best describes the noise observed in these stations.

Table 1: Types of monuments present in the RBMC of the studied GNSS stations.

Type of monument	Number of stations
Concrete pillar in building roof	58
Concrete pillar in the ground	40
Pillar in building structural column	7
Metallic tower in building roof	7
Others	7

Note that using a single noise model for all stations has the great advantage of allowing comparing the noise characteristics of each station that is part of the same network, assuming that, up to a certain level, all stations are affected by the same noise sources and, therefore, have a similar power spectrum (Williams *et al.*, 2004). However, it is suggested that different noise models should be considered depending on the application.

## 2.1 Estimation of velocity models by the WLS method and noise analysis by MLE

Velocity models can be estimated by the Weighted Least Squares (WLS) method, using the functional model expressed by Equation 1, where the parameters are estimated using the time series of GNSS coordinates. Simultaneously, the type and amplitude of stochastic noises are evaluated based on the residuals. This assessment is usually conducted to provide the most realistic estimate of uncertainties for velocity models.

The Maximum Likelihood Estimation (MLE) of noise shows the need to maximize the likelihood function by adjusting the covariance ( $C$ ) of the data. Thus, assuming a Gaussian distribution, the likelihood function ( $l$ ) can be given as (Williams, 2008):

$$l(x, C) = \frac{1}{(2\pi)^{\frac{N}{2}}(\det C)^{\frac{1}{2}}} \exp(-0.5\phi^T C^{-1}\phi) \quad (3)$$

$$\ln[l(x, C)] = \frac{-1}{2} [\ln(\det C) + \phi^T C^{-1}\phi + N\ln(2\pi)] \quad (4)$$

$$C = \sum_{i=1}^m \sigma^2 J_i \quad (5)$$

where  $x$  is the vector of observed data;  $J$  the covariance matrix for time-correlated noise, represented by a combination of different stochastic models;  $m$  is the number of stochastic models;  $\hat{\nu}$  the vector of residuals;  $N$  the number of observations; and  $\sigma^2$  the variance of the stochastic model.

If the covariance matrix consists of a noise source, then we have:

$$C = \sigma^2 J \quad (6)$$

$$\ln[l(x, \sigma)] = \frac{-1}{2} \left[ 2N \ln(\sigma) + \ln(\det J) + \frac{\hat{\nu}^T J^{-1} \hat{\nu}}{\sigma^2} + N \ln(2\pi) \right] \quad (7)$$

The considerations made allow us to assume that the estimated residuals and parameters (but not their uncertainties) do not change with a change of scale in the covariance matrix. In this case, Equation 7 can be derived regarding  $\sigma$  to find the value that provides maximum likelihood (Williams, 2008) by:

$$\sigma = \sqrt{\frac{\hat{\nu}^T J^{-1} \hat{\nu}}{N}} \quad (8)$$

If the covariance matrix  $C$  depends on more than one noise source, it must be transformed. Therefore, when two noise sources are present, a two-dimensional covariance matrix should only need a one-dimensional numerical maximization. In this case, two noise amplitudes can be transformed into two alternative variables (an angle " $\emptyset$ " and a scalar " $r$ ") and, for a given angle, it is possible to calculate a unit covariance matrix ( $C_{unit}$ ) that describes the correct ratios of these two variables.

$$\sigma_1 = r \cos \emptyset \quad (9)$$

$$\sigma_2 = r \sin \emptyset \quad (10)$$

$$C_{unit} = r^2 [\cos^2(\emptyset) J_1 + \sin^2(\emptyset) J_2] \quad (11)$$

## 2. The influence of different types of geodetic monuments present in the RBMC

This study used the daily time series solutions from 119 active stations of the Brazilian GNSS Continuous Monitoring available at the Nevada Geodetic Laboratory (NGL; Blewitt *et al.*, 2018) (Figure 1). These solutions, which make up the time series of station

coordinates, were referenced to IGS14 and estimated using the Precise Point Positioning method available in the GipsyX software, developed by the Jet Propulsion Laboratory of the California Institute of Technology.

The observation time of the selected stations is equal to or greater than 3 years (Figure 1), since observation periods shorter than three years may not show the effects to be modeled, according to Blewitt and Lavallée (2002) and Calais *et al.* (2006).

In addition to the daily solutions, the steps identified in the stations were included in the modeling of the time series (Equation 1). Steps (Figure 1) correspond to events where the station's position may have changed suddenly due to a change of either antenna or receiver, a seismic event, and any other factor that may interfere with the recording of the station's position, such as changes in the software. However, jumps only concern events where the source of the change in station position is known.

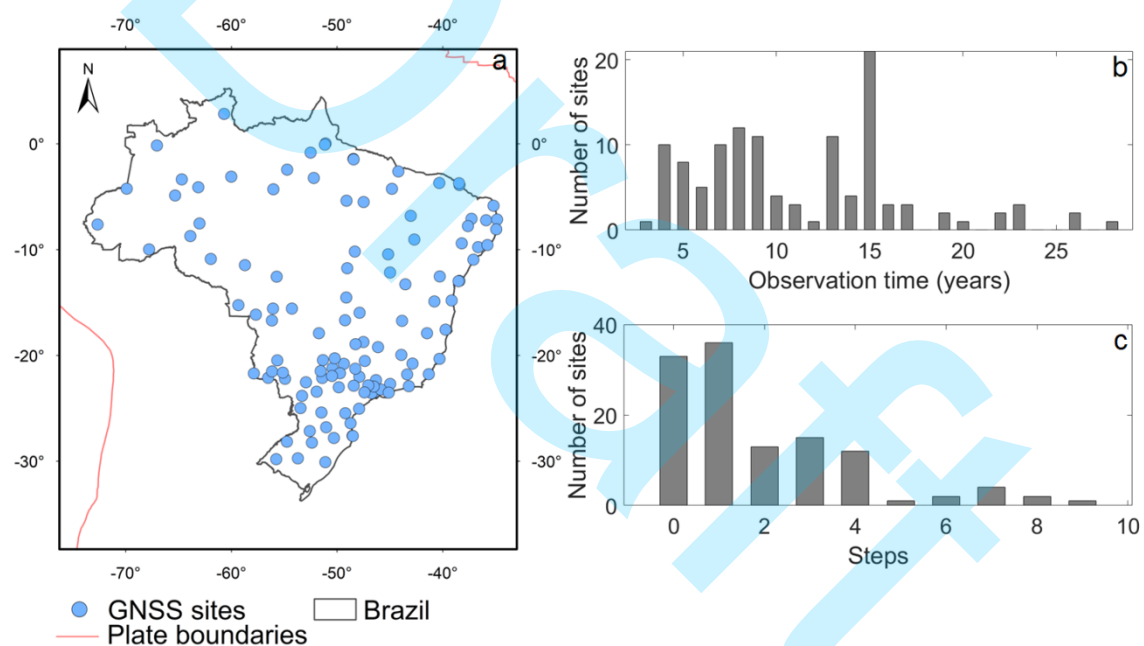


Figure 1: Stations of the Brazilian GNSS Continuous Monitoring (a). b) observation time of the GNSS stations. c) number of steps observed in the stations.

The noise observed in the time series of the selected GNSS stations was estimated and analyzed using the software CATS (Create and Analyze Time Series), developed by Williams (2008). This software allows both estimating and comparing stochastic noise processes in a continuous time series, using MLE analysis, as well as calculating the spectral index  $k$  of the time series through periodic position solutions.

In addition to the noise analysis, the speeds and uncertainties for the selected stations

were estimated by the WLS method, using different noise models, and combining the entire spectral indices. This approach is recommended for large networks of GNSS stations, where the combination of white noise and flicker (WN+FN) or white noise and random walk (WN+RW) is considered adequate to describe the noise present in most stations.

Finally, assuming no pre-established noise magnitude limit to characterize the instability of a station, a criterion was established for classifying a station as unstable regarding the monumentation or non-tectonic effects. To this, the spectral index  $k$  was analyzed for each component at each station, and the amplitude of the WN+RW noise was analyzed using the GESD (Generalized Extreme Studentized Deviation) statistical test, proposed by Rosner (1983), traditionally used to identify outliers.

The GESD (Rosner, 1983) used in this work is commonly applied to samples with approximately normal distribution, where it is necessary to define a limit  $R$  of possible outliers. In this study, any component of a GNSS station that presents a WN+RW noise amplitude greater than that defined by the statistical test was considered an outlier and, therefore, unstable compared to the other stations on the network. After defining the criteria,  $R$  tests are performed separately: one test for one outlier, one test for two outliers, and up to  $R$  outliers. The test null hypothesis is that there are no outliers in the sample. The alternative hypothesis is that there are up to  $r$  outliers.

$$R_i = \max \frac{x_i - \bar{x}}{s} \quad (12)$$

$\bar{x}$  and  $s$  are the mean and the standard deviation of the samples, respectively. The test was performed for each component of each station, at 95% confidence level. After calculating the first  $R$  statistic, with all observations, the observation that maximizes  $x_i - \bar{x}$  is removed and the test is performed again with  $n - 1$  observations until  $R$  tests are performed. The critical values for each test are calculated by the following equation:

$$\lambda_i = \frac{(n-i)t_{p,n-i-1}}{\sqrt{(n-i-1+t_{p,n-i-1}^2)(n-i+1)}} \quad i = 1, 2, \dots, r \quad (13)$$

where  $t_{p,n-i-1}$  is the percentage of the  $t$  distribution for  $n - i - 1$  degrees of freedom, and  $p$  is:

$$p = 1 - \frac{\alpha}{2(n-i+1)} \quad (14)$$

where  $\alpha$  is the test significance level. Finally, the number of outliers is defined by finding



the largest  $i$ , such that  $R_i > \lambda_i$ .

### 3. Results and Discussion

Figure 2 presents the spectral index in the north, east and vertical components (n, e, and u) for the GNSS stations studied. The average spectral index of the set of stations is  $k = -0.67$ ,  $k = -0.64$ , and  $k = -0.60$  for the n, e, and u components, respectively.

These results corroborate the conclusion that the combination of white noise and flicker best describes the noise of the set of RBMC stations as reported by Amagua *et al.* (2018) and Ramos *et al.* (2022). However, indices  $k < -1$  observed in the results (Figure 2) are further evidence that the random walk is also significantly present in some stations in the network.

The stations (BEPA, BRFT, SALU, SMAR), with  $k < -1$ , correspond to approximately 3% of the total. The noise amplitudes in these stations are higher for the WN+RW model compared to the WN+FN model (Table 2). However, it is understood that the uncertainties determined by the WN+RW model are more realistic considering the influence of the random walk on the time series. Of the stations mentioned, BEPA, SALU and SMAR presented index  $k < -1$  in the north and east components, thus highlighting the correlation between the horizontal components.

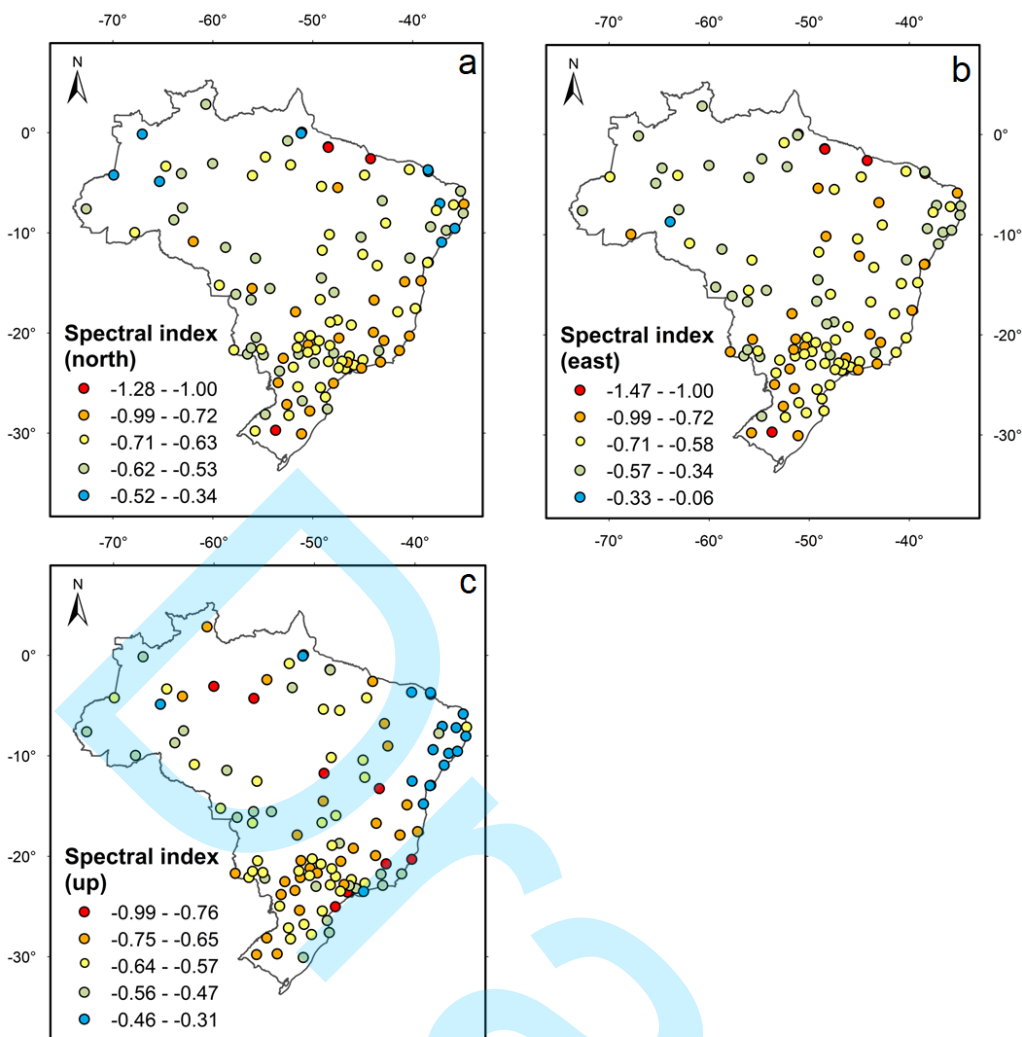


Figure 2: Spectral index of GNSS stations in the north (a), east (b) and up (c) components.

Table 2: Noise amplitude of stations with a spectral index lower than -1 in at least one component. RW+WN express the combined random walk and white noise model.

FN+WN refer to the combined white noise and flicker noise model.

Station	RW+WN ( $mm \times year^{-\frac{1}{2}}$ )			FN+WN ( $mm \times year^{-\frac{1}{2}}$ )		
	North	East	Up	North	East	Up
BEPA	20.66	26.12	12.05	9.48	10.27	11.72
BRFT	8.33	4.67	8.45	6.15	3.85	9.55
SALU	16.59	35.10	30.67	7.96	12.71	18.32
SMAR	28.19	46.97	19.96	10.12	11.93	15.95

The GESD test was applied to the 119 stations studied to identify instability. The maximum number of supposed outliers was defined at 20% of the total stations ( $R = 24$ ). If the calculated number of outliers is below this value, the test is complete. The statistical analysis was consistent since the number of outliers in each component was significantly below the number of tests performed. A total of 10 stations were classified as unstable since at least one component of the noise amplitude was an outlier (Table 3). Of these, BEPA, SALU and SMAR had already been classified as unstable because the northern and eastern components of the spectral index were lower than -1. Of the 10 stations, 6 were identified as outliers in the northern components, 7 in the eastern component and 3 in the vertical component (Table 3).

Table 3: Noise amplitudes were classified by GESD (Generalized Extreme Studentized Deviation) as outliers in the north, east and/or up components.

Station	Noise amplitude RW+WN ( $mm \times year^{-\frac{1}{2}}$ )		
	North	East	Up
BEPA	20.66	26.12	-
MGIN	-	8.84	-
NEIA	-	-	42.63
PIFL	-	9.68	-
POLI	-	-	66.38
PRCV	9.09	-	-
SALU	16.59	35.10	30.67
SCCH	12.70	15.55	-
SMAR	28.19	46.97	-
VICO	9.30	11.16	-

Soil contraction, compaction of aquifer systems, gravity-driven downward movements, pore-elastic effects, and monument deformation by thermal expansion or contraction are just a few examples of unmodeled factors that can influence the estimation of realistic uncertainties of GNSS velocities (Ferreira *et al.*, 2019; Calais *et al.*, 2006; Galloway *et al.*, 1999). Therefore, the strategy of using a combination of WN+FN for all stations, after removing those where the magnitude of WN+RW is classified as discrepant, can

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minimize the number of factors that affect the stochastic processes of the stations that will be used in tectonic and geodynamic studies.

The model that includes flicker noise, in addition to having already been indicated as more suitable for the RBMC, considers that the stations are subject, as a whole, to a common physical base, which may be affected by different seasonal phenomena, such as atmospheric and hydrological loads, atmospheric noise and/or second-order ionospheric effects (Kedar *et al.*, 2003; Dong *et al.*, 2002; Williams *et al.*, 2004).

The WN+RW magnitudes averaged  $5.79$ ,  $6.23$  and  $14.65 \text{ mm} \times \text{year}^{-\frac{1}{2}}$  in the northern, eastern and up components, respectively (Figure 3). These results agree with values presented in previous works, where the horizontal components are less noisy than the vertical ones (Mao *et al.*, 1999; Langbein, 2004; Amagua *et al.*, 2018).

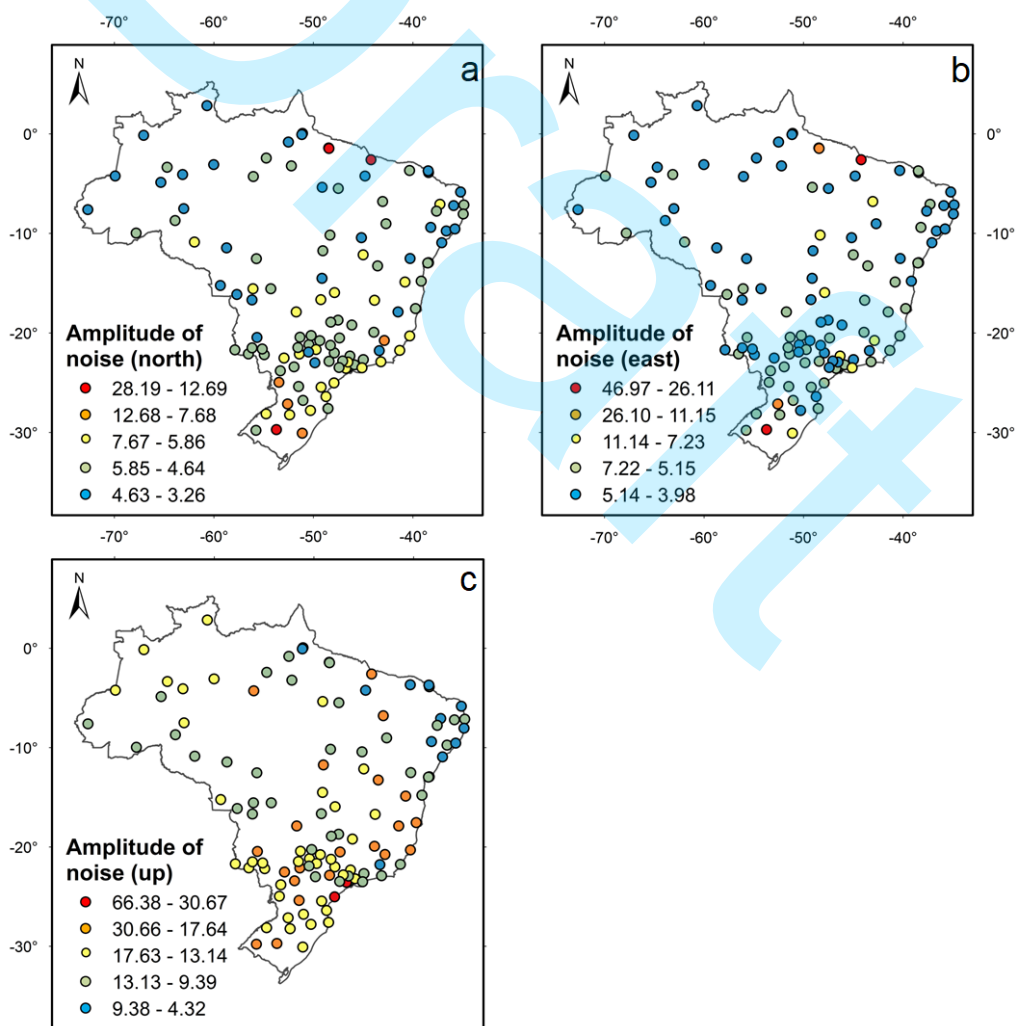


Figure 3: WN+RW noise amplitude, expressed as  $mm \times year^{-\frac{1}{2}}$ , in the north (a), east (b) and up (c) components.

Figure 4 shows the GNSS stations where at least one component of the noise magnitude was higher than statistically established, in addition to those where at least one component had the index  $k < -1$ . Of the stations whose  $k$  index was lower than -1, only the BRFT station was not classified as an outlier in the GESD test.

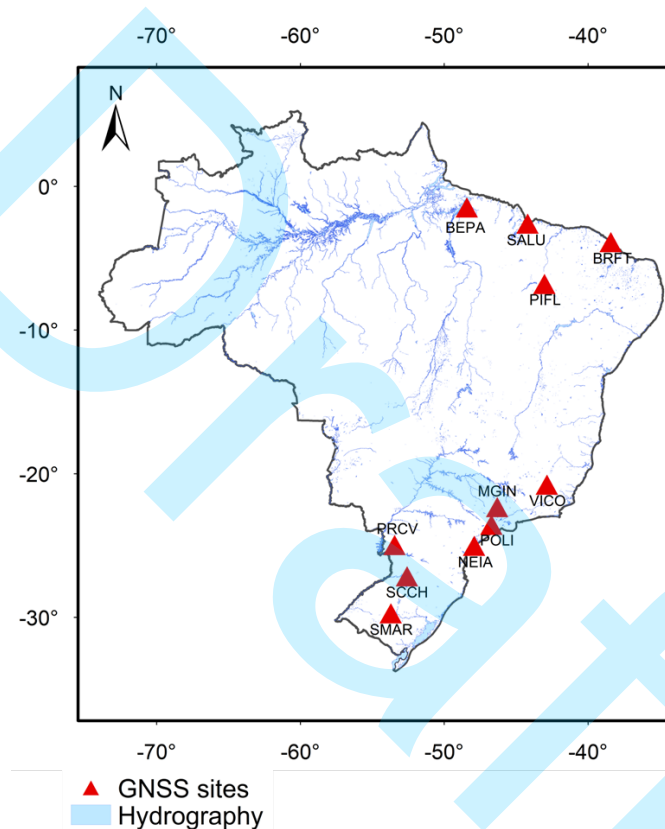


Figure 4: GNSS stations with spectral index or noise amplitude above the limits established for classification of monument stability.

Considering that white, flicker and random walk noises predominate in the high, intermediate and low frequencies of the power spectrum of the time series, respectively, we notice the presence of such noises in the 11 stations presented in Figure 4 (referred to as unstable from now on). Figure 5 shows this behavior, in which the signal power density, from a period of approximately  $10^3$  days, corresponds to the random walk. This result also evidences that a long observation period is necessary to characterize this type of noise. The northern component of the SALU station clearly illustrates the predominance of each type of noise in the power spectrum of the time series, as

mentioned previously.

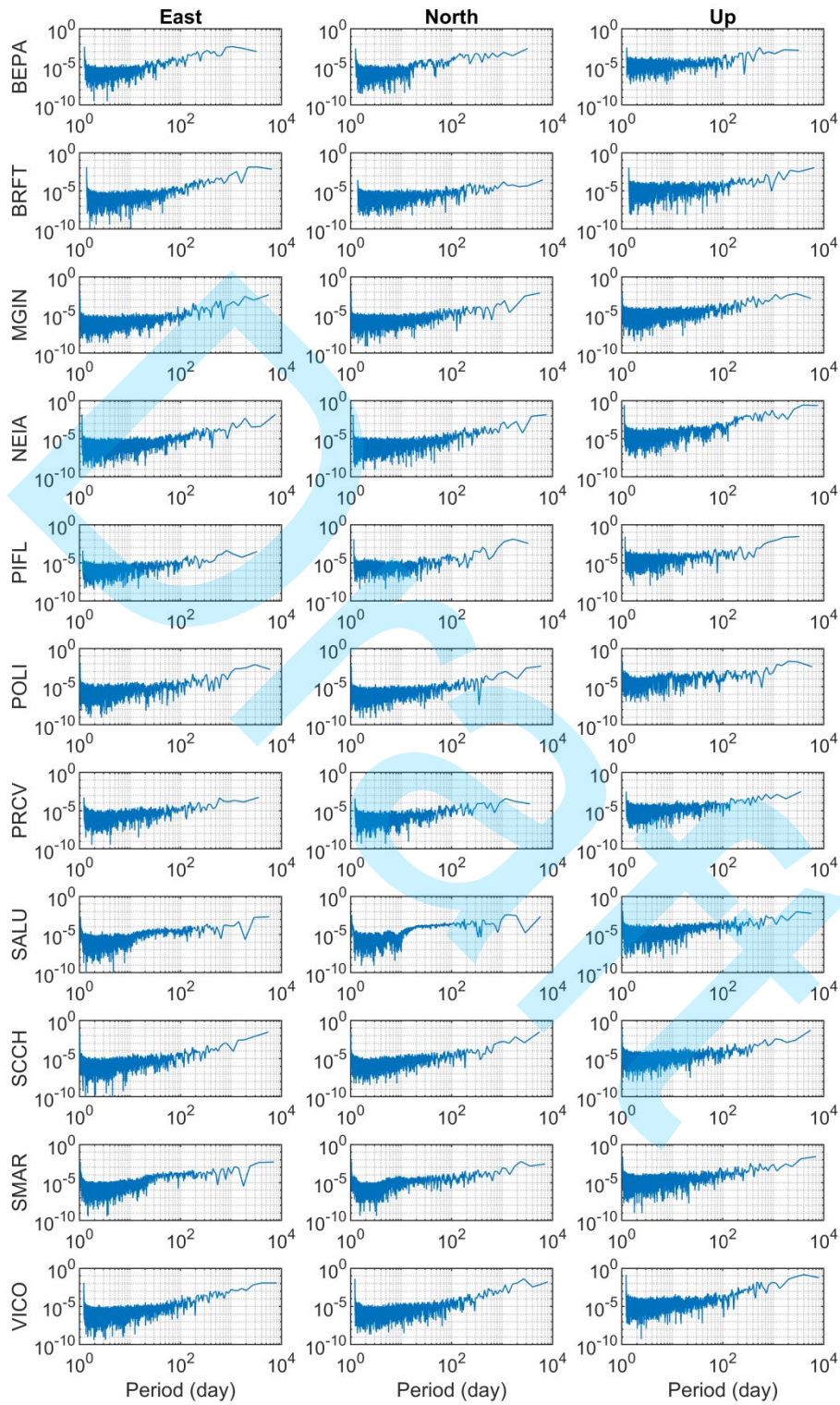


Figure 5: Power spectrum of the time series of the 11 unstable stations.

A total of 11 stations present noise magnitude greater than the statistically established value, or with a spectral index  $k < -1$  (unstable); of which 4 are either in coastal areas or river basins (Figure 4). This data corroborates previous results presented by Amagua *et al.* (2018), who stated that the stochastic properties of the time series of these stations may be influenced by typical signals from these locations, such as the effects of hydrological loads. The POLI station, with more than 16 years of observation, is located approximately 500 m from the Pinheiros River and is installed on a building slab and may be subject to various effects that cause instability.

Ferreira *et al.* (2022) conducted a study in Manaus, AM, and observed annual variations of about 5 meters in the groundwater level and suggested that this is the main source of local variations in the gravity signal. The station studied by the authors has several similarities with the stations classified as unstable in this study, such as being located in thick sedimentary basins, presenting unconsolidated sediments where the geodetic monument is located, and being close to rivers whose water levels vary widely.

Thus, it is possible to suggest that both results of the BEPA station, located in the Amazon hydrographic basin, and the BRFT, SALU and NEIA stations, located in coastal areas, can be influenced by local variations in the water level present in the soils and rocks.

The other 6 stations classified as unstable (MGIN, PIFL, PRCV, SCCH, SMAR and VICO) have at least 9 years of observation each. One hypothesis for identifying the instability of these stations is the longer the observation time, the greater the possibility of identifying random walk noise.

Also, more than 70% of the stations classified as unstable are located in oxisols or argisols (Table 4). Despite being deep soils, which could contribute to the instability of the station, 58% of the national territory is covered by these soil types (Santos *et al.*, 2018), therefore, it is not possible to directly correlate the soil type with the instability of these stations.

Table 4: Type of soil, monuments and observation time for removed stations. PBCS = Pillar on a concrete base on the ground. TMLE = metal tripod on a concrete slab of a building roof. PCLE = Concrete column on a building slab. TMS = Metallic tower on the ground.

Station	Soil	Monumentation	Observation time (years)
BEPA	Gleysol	TMLE	8.8
BRFT	Argisol	PBCS	17.63
MGIN	Oxisol	PCLE	15.33
NEIA	Cambisol	PCLE	20.85
PIFL	Argisol	PBCS	9.00
POLI	Argisol	TMS	16.20
PRCV	Oxisol	TMS	9.70
SALU	Oxisol	PCLE	15.70
SCCH	Neosol	PBCS	15.10
SMAR	Argisol	PCLE	19.34
VICO	Oxisol	PCLE	22.03

Table 4 shows the distribution of the 11 stations regarding the monument type. The data shows that the 7 stations classified as unstable have monument type “concrete pillar on a building slab” or “pillar on a concrete base on the ground”. However, it was not possible to correlate noise magnitude with the type of monumentation, since approximately 80% of the stations have these types of monumentation, a value similar to that observed in stations classified as unstable. Therefore, it is suggested that under the conditions presented, the analysis of the spectral index and noise magnitude of each station in the network, individually, tends to be the most appropriate strategy for classifying unstable stations in the Brazilian territory.

Furthermore, the shortest observation time of stations classified as unstable is 8.8 years (BEPA) (Table 4). This raises the hypothesis that stations with shorter observation times do not allow to characterize the random walk appropriately, due either to the magnitude of white and flicker noise or other factors. Klos *et al.* (2018) identified that the noise character becomes more important than seasonal signals after 9 years of continuous observations. In this case, it is suggested that, for application in geodynamic and tectonic studies, the minimum observation time of ~9 years for the RBMC should be considered



to be able to identify and classify the different types of noise.

Figure 6 presents the estimated horizontal velocities model for the stations, considering the noise model that combines white and flicker noises. The average velocities are 13 mm/year, with a standard deviation of 0.7 mm/year. The horizontal components' average velocities are 12 mm/year in the northern and -3 mm/year in the eastern components, and standard deviations of 0.6 and 0.7 mm/year, respectively.

These velocities show that the South American intraplate is in fact stable, which can also be observed in other previously velocity models (e.g., Ramos *et al.*, 2021; Marotta *et al.*, 2013b). Sánchez and Drewes (2020) identified that the only stable regions in Latin America are the Brazilian, Guiana and Atlantic shields. The fact that the estimated velocities agree in magnitude and direction shows that the regional component of plate movement is predominant. Therefore, for studies of local stresses and strains, it is necessary to remove the regional component and analyze the residual components, which may not be suitable for this purpose, depending on the level of estimated uncertainties.

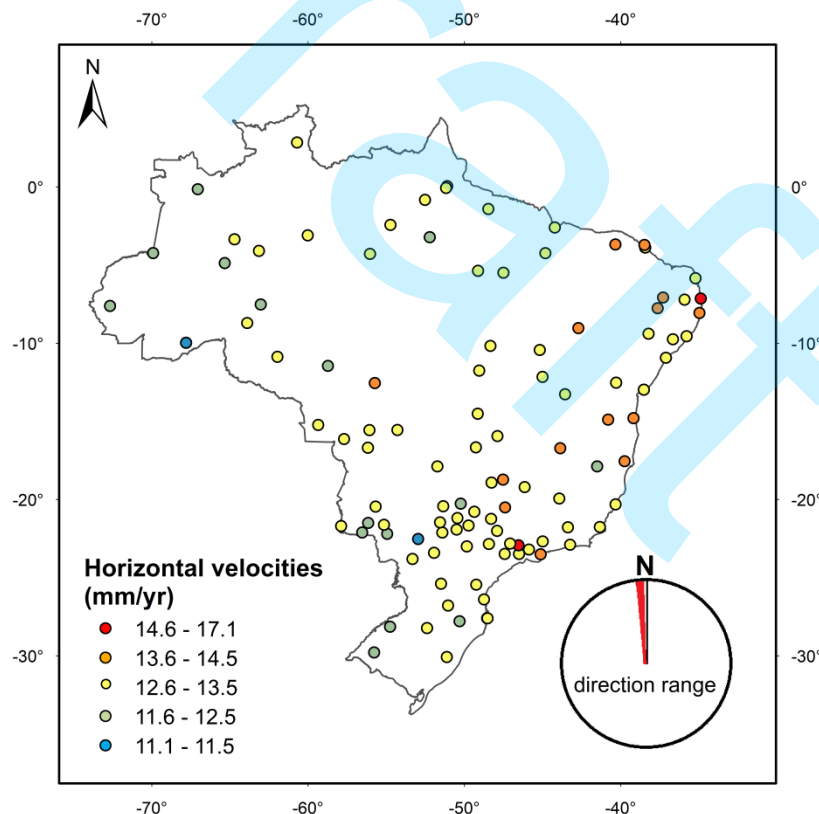


Figure 6: GNSS horizontal velocities model. The noise model used combines white noise and flicker noise.

#### 4. Conclusion

The evaluation of 119 GNSS stations located around the Brazilian territory indicates a significant presence of random walk noise in some of these stations, detected from the analysis of the noise magnitude using a model that combines white noise and random walk and, also, in the analysis of the spectral index of the stations.

However, the analysis of elements such as location and type of geodetic station monuments showed that local factors, known or unknown, individually affect the stability of GNSS stations and, therefore, hinder/hamper the full modeling of the data behavior. Thus, it is suggested that adopting a quantitative strategy for characterizing and removing stations considered unstable can provide better quality for tectonic and geodynamic studies.

Regarding the stations where instability of the geodetic monument was identified, most are in coastal areas or under the influence of large watercourses. In these locations, a variety of factors may be contributing to the instability of the GNSS station, such as, for example, variations in water level, the presence of unconsolidated sediments, or local atmospheric effects.

Additionally, since the stations with detected instability of the monument cover an observation period of at least eight years and the identification of the random walk noise depends on the amount of data, it may be suggested that the stations with an observation period between three and eight years may also have been affected by this type of noise which, however, was not characterized properly due to the inadequate length of the time series. In conclusion, we suggest that, in tectonic and/or geodynamic applications, only stations with more than 9 years of observation should be used in Brazil.

#### 5. References

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