

EXPLORATORY FAVORABILITY CLASSIFICATION USING WEIGHTS OF EVIDENCE: A CASE STUDY IN SERGIPE-ALAGOAS BASIN, BRAZIL

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ABSTRACT. This article discusses the importance of the favorability evaluation, proposed in data-driven mineral potential maps (MPM), for decision-making in exploratory activities of petroleum and natural gas. We consider geophysical and geological information as evidences that define the essential elements of a petroleum system. We assess such evidences by means of weights of evidence methodology, which makes use of data coming from hydrocarbon discovering wells. We apply the proposed assessment in a case study in Sergipe-Alagoas and employ the results to classify areas of interest in different favorability levels.

Keywords: petroleum systems, favorability maps, mineral potential maps, Sergipe-Alagoas basin.

RESUMO. Este artigo discute a importância da avaliação de favorabilidades propostas em mapas de potencial mineral, baseados em dados (*data-driven*), para as tomadas de decisões em atividades exploratórias de petróleo e gás natural. Nós consideramos as informações geológicas e geofísicas como evidências que definem os elementos essenciais de um sistema petrolífero. Avaliamos as evidências através da metodologia de pesos de evidências (*weights of evidence*), a qual faz uso de dados obtidos a partir de poços descobridores de hidrocarbonetos. Aplicamos a avaliação proposta em um estudo de caso na bacia de Sergipe-Alagoas e empregamos os resultados obtidos para classificar a área de interesse em diferentes níveis de favorabilidade.

Palavras-chave: sistemas petrolíferos, mapas de favorabilidade, mapas de potencial mineral, bacia de Sergipe-Alagoas.

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INTRODUCTION

The use of geophysical methods is very important for petroleum system evaluation during exploratory activity. The information acquired from the available data regarding the area under analysis is critical for the decisions made in the exploration, and the acquisition of new data may produce a relevant cost in exploratory investments that have a high-risk exposure.

Despite the consensus that more data always contributes to reduce uncertainties, exploratory data typically provides imperfect information which drive the decision-making process (Sato et al., 2013; Rostirolla, 1997). Such information can be furnished by mineral-potential maps (MPM), which strive to spatially indicate more favorable regions to survey for mineral deposits (Bonham-Carter, 1994; Harris & Pan 1999; Singer & Kouda, 1999; Brown et al., 2000; Brown et al., 2003; Harris et al., 2003; Porwal et al., 2003, 2004; Agterberg & Bonham-Carter, 2005; De Quadros et al., 2006; Abedi et al., 2012; Magalhães & Souza Filho, 2012; Pazand et al., 2013).

The favorability quantification in mineral exploration can be subdivided in two types of models, according to the mechanism used to associate the hydrocarbon accumulations with selected geological factors (Pazand et al., 2013): (1) knowledge-driven models and (2) objective quantification based on data, depending on the availability of the data and on the exploratory stage of the area of interest.

Evaluation methods based on data (Newendorp, 1972; Bonham-Carter, 1994; Moon, 1998; Cheng & Agterberg, 1999; Carranza & Hale, 2001; Porwal et al., 2003; Carranza et al., 2008; Cassard et al., 2008) propose to establish, in an empiric manner, the relationship among factors observed on indirect evidences in geological, geophysical, and geochemical data and on the known accumulations. It is this relationship that is used to assess the exploratory favorability in areas being surveyed. The favorability indices are obtained based on evidences spatially organized in maps, which analyze petroleum system factors selected from data acquired in the area of interest. The importance of each evidence is evaluated based on the results observed and consolidated in a favorability map for the area (Harris et al., 2001; Harris & Pan, 1999). The MPM technique allows the integration of data from different knowledge areas (geology, geophysics, geochemistry, and well data), and, for this reason, it presents considerable importance in exploration (Porwal, 2006; Carranza, 2011).

The relevance of this work is associated to the lack of information and the need to expand the geophysical and geological data acquisition in the Brazilian sedimentary basins. After a long monopoly period in the Brazilian exploration and produc-

tion (E&P) sector, the enactment of the Petroleum Law established regulatory changes that favored the expansion of data acquisition activities in the Brazilian sedimentary basins, and in addition established the Brasil-Rounds with the purpose to expand investments in the sector. The areas to be offered are promoted with data acquisition by means of a Geologic and Geophysics Plurianual Plan (Anp, 2014), developed to increase the knowledge about the potential of the Brazilian sedimentary basins, with surveys of geological and geophysical technical data.

Mineral resource evaluation depends on the data acquisition in regional surveys (Jordanov et al., 2006). Moreover, operational research represents an important tool that makes use of these data to support the scheduling of exploratory and additional data acquisition activities (Cobb, 1960). In this work, we apply weights of evidence based on model proposed by Bonham-Carter, Agterberg and Wright (1990) to produce exploratory favorability maps. We employ the proposed technique to a case study in the Sergipe-Alagoas basin, which presents aspects about the tectonostratigraphic evolution and its confirmed petroleum systems. The numerical experiments indicate that the proposed evidences are related to the results of successful exploratory wells, i.e. those with identified discoveries. Furthermore, the model allows a careful classification of the area according to its exploratory favorability, and can be used to support exploratory decisions, data acquisition and selection of prospective exploration areas. In a regional perspective, when there is a lack of data, the less favorable areas may be subject to surveys for data acquisition or area relinquishment, whereas the more favorable areas are naturally attractive for future bidding round offers.

This work is organized as follows: Section 2 – Methodology – proposes a weights-of-evidence model of exploratory favorability. Section 3 – Case Study – applies the proposed model for the Sergipe-Alagoas basin. Section 4 – Results – is comprised of the numerical experiments for the case study. Finally, Section 5 – Conclusion – concludes the paper.

METHODOLOGY

The weights-of-evidence (WOFE) technique allows the identification of patterns, such as structural features and geophysical and geochemical anomalies (Bonham-Carter et al., 1990), to map mineral potential (Agterberg, 1992; Cheng, 2014; He et al., 2014). It was employed to search for gold (Bonham-Carter et al., 1988; Harris & Pan, 1999; Brown et al., 2000; Carranza & Hale, 2002; Cheng et al., 2007; Hronsky & Groves, 2008; Carranza, 2011; Silva et al., 2012; Ford & Hart, 2013), groundwater (Vidal et al., 2005; Nampak et al., 2014; Pourtaghi & Pourghasemi, 2014),

copper (Abedi et al., 2014; Wenhui et al., 2014) and iron (Sato et al., 2013; Zhang et al., 2013).

For petroleum and natural gas (P&NG) exploration, the WOFE technique usage is based on the petroleum system concepts and on exploratory plays, with the purpose of reducing the exposure of data acquisition investments to the exploratory risk, using probability theory (Rostirolla et al., 2003). This method was also employed for rockslide evaluations (Blahut et al., 2013) and landslide susceptibility (Blahut et al., 2009; Regmi et al., 2014; Kouli et al., 2014), among others.

Consider an area of interest $t > 0 \text{ km}^2$, divided into grids (cells) of constant area $u > 0 \text{ km}^2$. Clearly, $T = t/u$ is the number of cells in the area. If the area presents D number of cells with confirmed occurrences of reservoirs, the prior probability that a randomly selected cell presents an occurrence is defined as $P(Oc) = D/T$. With regards to the considered evidences within the area of interest, the model calculates the number of cells B_j found in each evidence map J , where this evidence is present; the number of cells where the evidence is not observed is expressed by the term $\overline{B}_j = T - B_j$.

The conditional probability of selecting a cell with a reservoir occurrence, given that B_j cells presented evidence map J , is defined as $P(Oc/B_j) = \frac{|B_j \cap Oc|}{|B_j|}$, where $|A|$ denotes the cardinality of set A . On the other hand, the probability of not finding a reservoir given that B_j cells have evidence j is $P(\overline{Oc}/B_j) = \frac{|B_j \cap \overline{Oc}|}{|B_j|}$. The conditional probabilities that a reservoir is found or not, given that B_j is absent, are similarly calculated as

$$P(Oc/\overline{B}_j) = \frac{|\overline{B}_j \cap Oc|}{|\overline{B}_j|} \text{ and } P(\overline{Oc}/\overline{B}_j) = \frac{|\overline{B}_j \cap \overline{Oc}|}{|\overline{B}_j|}.$$

Bayes' theorem yields that,

$$P(Oc/B_j) = \frac{P(B_j/Oc)P(Oc)}{P(B_j)} \quad (1)$$

$$P(Oc/\overline{B}_j) = \frac{P(\overline{B}_j/Oc)P(Oc)}{P(\overline{B}_j)} \quad (2)$$

The contributing value of prediction for each evidence J is its weights value, defined as:

$$W_j^+ = \frac{P(B_j/Oc)}{P(B_j/\overline{Oc})} \quad (3)$$

$$W_j^- = \frac{P(\overline{B}_j/Oc)}{P(\overline{B}_j/\overline{Oc})} \quad (4)$$

For each evidence, W^+ and W^- indicate, respectively, the weight value of existent and non-existent evidence J as a measure

of importance of its presence for the D occurrences of reservoir represented in the posteriori probability map, as represented in Figure 1.

Another concept used is the odds ratio

$$O(Oc) = \frac{P(Oc)}{1 - P(Oc)} = \frac{D}{T - D},$$

which is defined as a ratio of the probability that an event will occur to the probability that an event will not occur. As to the evidence J , its odd is $O(Oc/B_j) = O(Oc) \cdot \frac{P(Oc/B_j)}{P(\overline{Oc}/B_j)}$. It is these values that ultimately define the favorability of each cell, which appears in the favorability map. If more than one evidence is present, Equation (5) defines the posteriori probability log, where n is the number of evidences considered:

$$\begin{aligned} & \log(O(Oc|B_1, B_2 \cdots B_n)) \\ &= \sum_{j=1}^n W_j^+ + \log(O(Oc)) \end{aligned} \quad (5)$$

CASE STUDY IN SERGIPE-ALAGOAS BASIN

The Sergipe-Alagoas basin is located in the northeast of Brazil and its area is around 46.000 km² in its largest emerged part (Loureiro, 2013). To the North, it is limited by the Pernambuco/Paraíba basin by means of the Alto de Maragogi; to the South, the emerged part is limited by the Estância platform and, in the ocean, it is limited by the Jacuípe basin, by means of the Vaza-Barris fault system. It presents a large variety of confirmed hydrocarbon accumulation models, with petroleum and natural gas production.

Tectonostratigraphic Evolution

The Sergipe-Alagoas basin has the most complete stratigraphic sequence of the Brazilian east continental margin. According to Feijó (1994a), Moriak et al. (1997, 1998), Azambuja Filho et al. (1998) and Souza-Lima et al. (2002), the Sergipe-Alagoas basin presents five tectonossequences: syncline, pre-rift, rift, transgressive drift and regressive drift.

According to Moraes Rego (1933), the basin bedrock belongs to the Proterozoic Eon and it is composed by low-grade metamorphic rocks of the Miaba and Vaza-Barris Groups in the Sergipe sub-basin.

The first tectonossequence was deposited during the Paleozoic syncline. In this period, represented by the Permian-Carboniferous sediments, the Batinga Formation and the Aracaré Formation were deposited. The Batinga Formation encompasses the following members: Mulungu, formed by conglomerates and

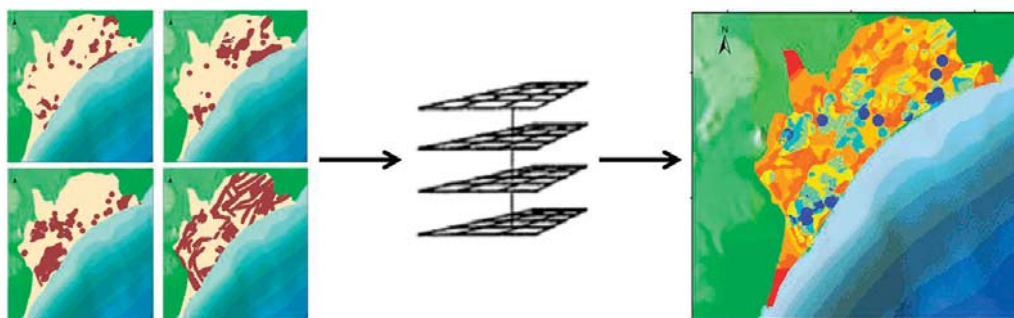


Figure 1 – Exploratory favorability map of Sergipe-Alagoas basin.

diamictites; Atalaia, formed by sandstones; and Boacica, composed of siltites and shales. The Aracaré Formation was deposited in a desertic and deltaic environment, under eolic and wave reworking (Campos Neto et al., 2007), and it comprises black shales covered by sandstones, calcarenites associated with silex and algae mudstone. Its total organic carbon (TOC) varies between 2 and 5% (Cruz, 1994a).

The second tectonossequence, the pre-rift, is marked by the alternance between fluvial and lacustric environments of the Early Jurassic Candeeiro and Bananeiras Formations. Sandstones and reddish siltites characterize the Candeeiro Formation, and the Bananeira Formation is marked by violet red shales, easily weathered.

The third tectonossequence, the rift, occurred from Berriasian up to Aptian. In the beginning of the rift phase, there was a progressive subsidence of the basin, with high pluviosity and erosion decrease in the source areas, in the distal portions of a fluvial system grading for lacustric deltaic fronts of the Serraria Formation, composed by coarse-grained to conglomerate sandstones. In this work, this formation was extracted from the pre-rift phase, as it is used in the stratigraphic chart developed by Campos Neto et al. (2007), and was added to the rift phase and to the Coruripe Group, like the other formations of the rift phase.

Also, in the continental environment of fresh or salty water, in a lagoon context, intercalations of underlapping sandstones and shales of Barra de Itiúba Formation were deposited. At the same time, the Penedo Formation was deposited from deltaic front to prodelta environments and it is composed by fine to coarse-grained sandstones that are locally conglomeratic, well to poorly sorted with subordinate intercalations of shales and siltites.

In the period that occurred from Valanginian to Aptian, a depositional system of this unit was formed. It is interpreted as alluvial fans associated with the border faults of the basin, actives on the Aratu to Jiquiá stages (Feijó, 1994a). It is called Rio Pitanga

Formation and is characterized by large conglomeratic wedge adjacent to the large border faults of the Sergipe sub-basin. Above the Jiquiá unconformity, short duration deltaic fans were developed near to lakes in Early Aptian (Cruz & Abreu, 1984). They were the responsible elements for the deposit of the sediments of the Coqueiro Seco Formation. This formation is marked by the alternance of sandstones, shales and siltites, and presents, in its bottom part, calcilutites and coquinas (Morro do Chaves Member) intercalated with conglomerates, sandstones and black shales.

The Maceió Formation is composed by intercalations of fine to coarse-grained arkoses which are locally conglomeratic, light gray to light yellow and brown, with greenish or dark gray shales and, to some extent, bituminous. In addition, interlamination of anhydrite and dolomite may subordinately occur, besides the halite layers. The latter ones are informally called "Paripueira evaporites". Probably, there is a correlation between the deposits developed with the alternance between the phases of humid and arid climate. In the humid period, there would be a larger siliciclastic supply from the continent, as a result of the floods in the lake, favoring the deposition of proximal deltaic fans and subaqueous turbiditic fans, with wooden organic matter, in the lake. During all Aptian, in the dryer periods, the siliciclastic inflow would be smaller, originating shales and calcilutites with algal mats, with high content of amorphous organic matter (up to 17%). The evaporites of this unit would have been deposited during the extreme dry periods (Arienti, 1996).

In the Late Aptian, there was the deposition of the Muribeca Formation which presents geologic layers very diversified, being directly related to the lithofacies and each one of its members, as a result of the very peculiar variations of the depositional systems. The Carmópolis Member contains polymitic conglomerates, diamictites, conglomeratic sandstones, sandstones, ritmites, calcilutites and shales. The Ibura Member comprises the largest part of the evaporitic section of the Muribeca Formation. It is

composed by many evaporitic cycles, which began by the deposition of carbonates and sulphates (anhydrite), followed by the precipitation of halite and mixed deposits of halite-sylvite, called sylvinites. Some cycles evolved into extreme dry conditions, depositing rare and extremely soluble salts, like carnallite and taquidrite. The Oiteirinhos Member is composed by the alternance of shales and peloidal calcilutites or microbial limestones. Its origin is interpreted as being related to the marine sediments deposited in the less constrained portions, external to the evaporitic basin.

After, Feijó (1979) proposed its update to a group, adding in it the Poção, Maceió and Muribeca Formations. So, the lithostratigraphic units corresponding to the Rift and Transitional stages of the basin were included in the Coruripe Group. After this, in the Late Alagoas, there were a strong tectonism and delimitation of the hinge line (Campos Neto et al., 2007).

The Maceió and Muribeca Formations determine the end of the rift tectonossequence and are characterized by the first expressive marine incursions, which represent the definitive break-up of Africa and South America, where the first evaporitic deposits occur.

The fourth tectonossequence is the transgressive drift and it comprises all units deposited due to thermal subsidence and sedimentary overburden. Cotinguiba and Piaçabuçu are the formations deposited in this phase, from the end of Aptian up to Coniacian. The Sergipe Group base establishes the beginning of the Drift stage in the Sergipe sub-basin, with the implementation of the carbonatic platform systems that mark the Brazilian Atlantic Margin.

The three members that compose the Riachuelo Formation represent different depositional contexts that integrate themselves to compose a wide mixed carbonatic platform. Being so, the geologic layer variations that occur inside this platform by the proximal and distal positioning are much more reflected by these units: the Maruim and Taquari Members respectively.

The Maruim Member is represented by normally thick strata, composed by calcarenites (grainstones to packstones), mainly oncolitic, locally presenting bioclastic, peloidal or oolitic composition; in some cases, the carbonatic banks are represented by the calcirudites.

The Cotinguiba Formation is composed of only the Aracaju Member, which is represented by argillites and/or gray to green, calciferous, fossiliferous siltites, with intercalations of brown, bituminous shales and yellow crypto-crystalline limestones (Bengtson, 1983).

The fifth tectonossequence is the regressive drift, which occurred from Santonian to Recent, and is represented by the

Piaçabuçu Group. It holds the Marituba, Mosqueiro, Calumbi and Barreiras Formations. Locally dolomitized, the first formation deposited, the Marituba, is mainly composed by medium to coarse-grained conglomeratic sandstones, with intercalations of bioclastic calcarenites, sandy calcarenites and shales. It is supposed that the genesis of this unit is related to the coastal deposits distributed from Campanian to Recent. In the case of Mosqueiro Formation, it is mainly composed by bioclastic gray calcarenites. Shells of foraminifera and molluscs dominate the bioclasts. Thin intercalations of shales and coarse-grained sandstones are casually found. This unit represents the carbonatic platform, which was active from Paleocene to Holocene in the Sergipe sub-basin (Feijó, 1994a). Then, the deposits of the Calumbi Formation, supposed to have been generated in the platform region, are essentially represented by shales and argillites, with some intercalations of siltites. Relatively narrow bodies of fine to very fine-grained sandstones sporadically occur intercalated between shales and siltites; they are light yellowish brown coloured and very bioturbated. These sandstones were interpreted as resulting from the reworking of sandbars by the action of waves, that experience sea floor spreading, in more distal areas of the platform (Souza-Lima, 2001a). Finally, the Barreiras Formation (from Miocene to Recent) is mainly marked by sandstones, whose granulometry varies from fine to very coarse, ortoconglomerates and, secondarily, argillites and oxidized shales.

In this article, the study area focuses on the onshore portion of the Sergipe sub-basin. Since it is a mature basin, there is abundant information and, hence, geological knowledge. Figure 2A shows the stratigraphic chart with tectonossequences used in this study and Figure 2B shows the schematic section of the basin.

Petroleum System

Three main units represent the source rocks: Barra de Itiúba Formation, Coqueiro Seco and Aptian Maceió. The main source rocks of the basin are black shales, marls and calcilutites of the Maceió Formation. The average value of total organic carbon of the shales is 3.5%, reaching up to 12%. The average thickness of this unit is 200 m, reaching up to 700 m. Other important sources are the lacustrine shales of the rift phase, with possible marine influence, of the Coqueiro Seco Formation, and the lacustrine shales of the pre-rift and rift phases of the Barra de Itiúba Formation.

With regards to the reservoir rocks, the main reservoirs are in the clastic sediments of the Carmópolis Member of the Muribeca Formation. Also, there are sandstones presenting optimal porosity in the Cretaceous turbidites of the Calumbi Formation. Accumulations are found in the fractured basement and in the reservoirs of the rift phase – the porous and fractured carbonates of

bottom part of the Alagoas hinge. The migration occurred from this point by common faults, that compose the Alagoas hinge, up to Carmópolis Member, capped by the shales and evaporites of the Ibura Member of the Muribeca Formation. The latter acted as the carrier layer of petroleum up to its final accumulation in traps, usually paleogeomorphic. The largest field of the basin, Carmópolis, with 268 million cubic meters of *in situ* original oil, was supplied by this source with long-distance lateral migration. The gravitational (listric) and common faults played an important role. During the rifting of the basin, they were active and, moreover, they worked like pipelines for hydrocarbon migration.

The traps, researched in the pre-rift and rift sequences, are dome structures, like the Pilar and São Miguel dos Campos Fields. In the transitional sequence, the traps related to the Muribeca Formation/Carmópolis Member are mainly paleogeomorphic. In the sandstones of the Maceió Formation, the existent traps are fault blocks, or associated with halokinesis. In the upper sequence, the main reservoirs are the Cretaceous and Tertiary turbidites of the Calumbi Formation, the traps are mixed and stratigraphic, associated with the troughs and warpings caused by the salt tectonics or by the channel fill, sometimes controlled by basement reactivated faults.

Dataset and Variables

The selection of variables that have useful information to distinguish potentially productive areas is a crucial step for the geologic risk assessment. This study considered the maps hereinafter presented (UFRN, 2008) for the proposition of the evidences for the Sergipe sub-basin.

The Sergipe sub-basin has 4,583 drilled wells, of which 992 are for exploration and 3,591 for the production development (482 drilled offshore, 4,101 onshore); the Alagoas sub-basin has 910 drilled wells, of which 385 were drilled for exploration and 525 for petroleum production (864 onshore, 46 offshore) (BDEP-WEBMAPS, 2014). The hydrocarbon occurrences were defined from well reclassification data, and 715 exploratory wells were considered to be points with known hydrocarbon reservoirs.

The maps presented from Figure 3 to 7 were based on integration of the seismic (interpretations of seismic sections) and gravimetric (correlation between the gravimetric signal and high levels of basement or volcanic structure) data with the well data (conversion of in depth seismic maps from checkshot profiles, using time \times depth curves).

The methodology was applied based on geological criteria, as follows: presence of reservoir rocks and seal elements of petroleum systems, presence of large amounts of sediment, structural highs and faults. The presence reservoir rocks and seal can

be evidenced by thicker regions tectonosequences shown in Figures 3, 4 and 5. The pre-rift, indivisible and rift tectonosequences were chosen because they have representative rocks regarding the main plays in onshore Sergipe sub-basin. The bouguer anomaly values presented on Figure 6 were considered to identify regions according with its sedimentary thickness. Regarding structural high, the top of the crystalline basement were considered on Figure 7, since there may anticline structures nearby. Lastly, the faults were considered due to its possible contribution to hydrocarbon migration to the reservoir.

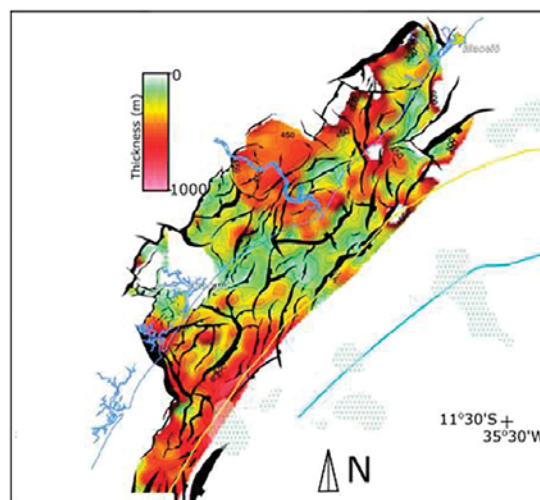


Figure 3 – Seismic structure and isopach map of the Pre-rift tectonosequence.

The thickness were estimated in each isopach considering interpolated information for each horizon based on krigging mathematical models, in which the isopach map was acquired from the difference between two in depth consecutive structural maps.

The analysis carried out by the model considered the data obtained from 487 exploratory wells with discoveries (BDEP-WEBMAPS, 2014) for the evaluation of the evidences analyzed from the maps presented in Figure 3 to 7. The wells that presented discoveries in the sedimentary layers were properly taken into account in the proposed evidences, with an arbitrated influence area of 2.5 km. Table 1 presents the proposed evidences and the adopted criteria, together with the area and number of exploratory wells presenting hydrocarbon discovery (D) for each analyzed evidence.

We implemented the weights of evidence model supported by a georeferenced structured database, developed specifically for this purpose.

The exploratory evidences were considered in georeferenced discretized binary layers, generated from maps presented in Figures 3 to 7. Those layers were created based on criterias presented in Table 1 and presented in Figure 8.

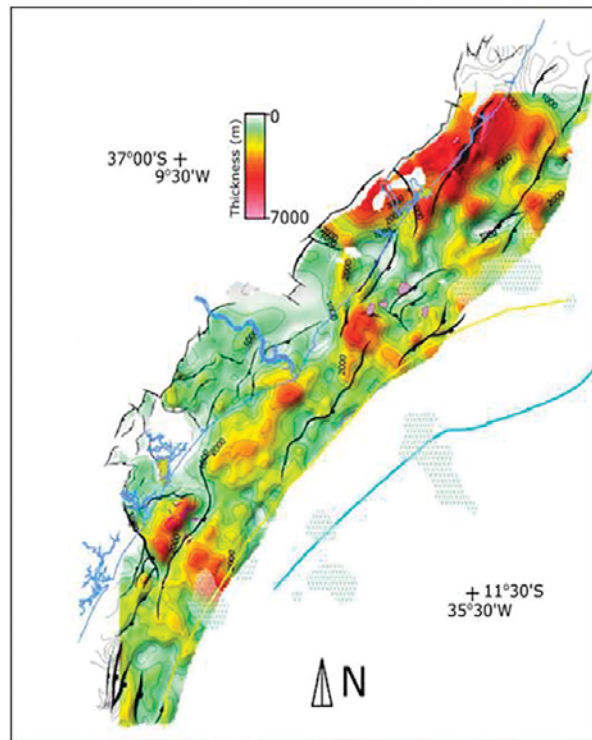


Figure 4 – Seismic structure and isopach map of the Indivisible tectonosequence.

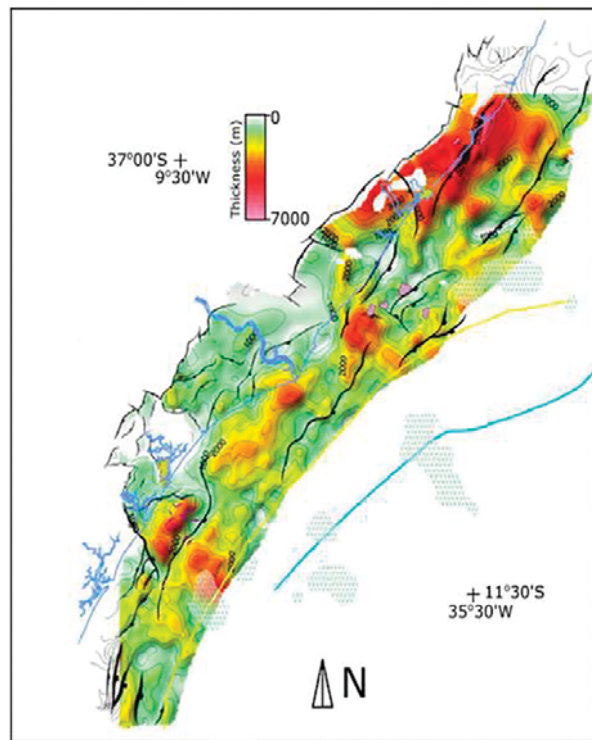


Figure 5 – Seismic structure and isopach map of the Rift tectonosequence.

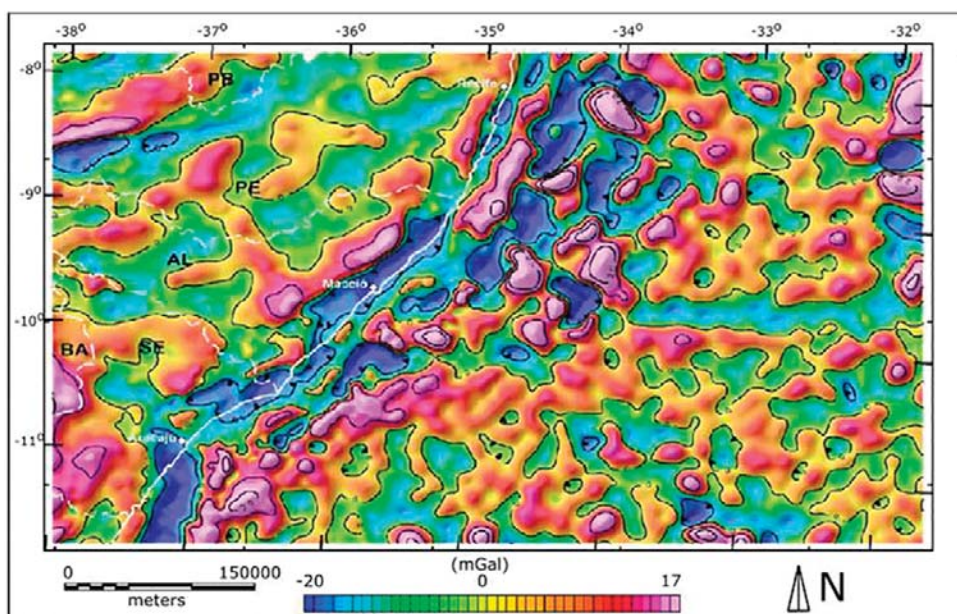


Figure 6 – Residual Bouguer Anomaly Map (the white line is the coast line). This map was generated from band pass between 10 and 100 km.

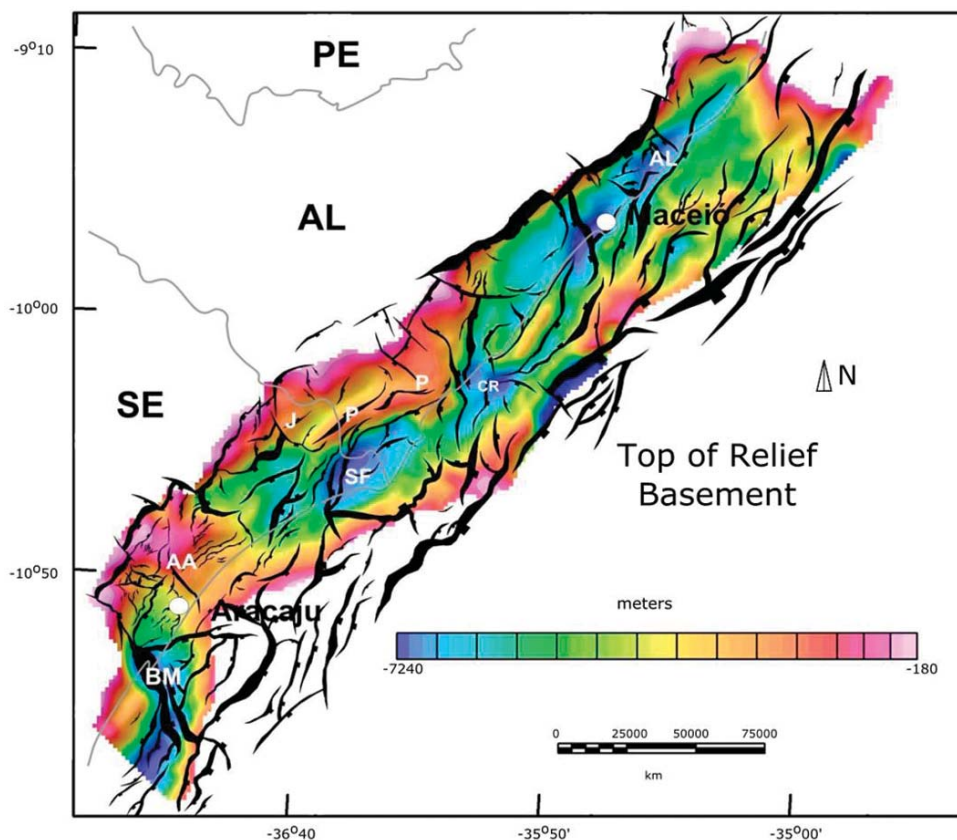
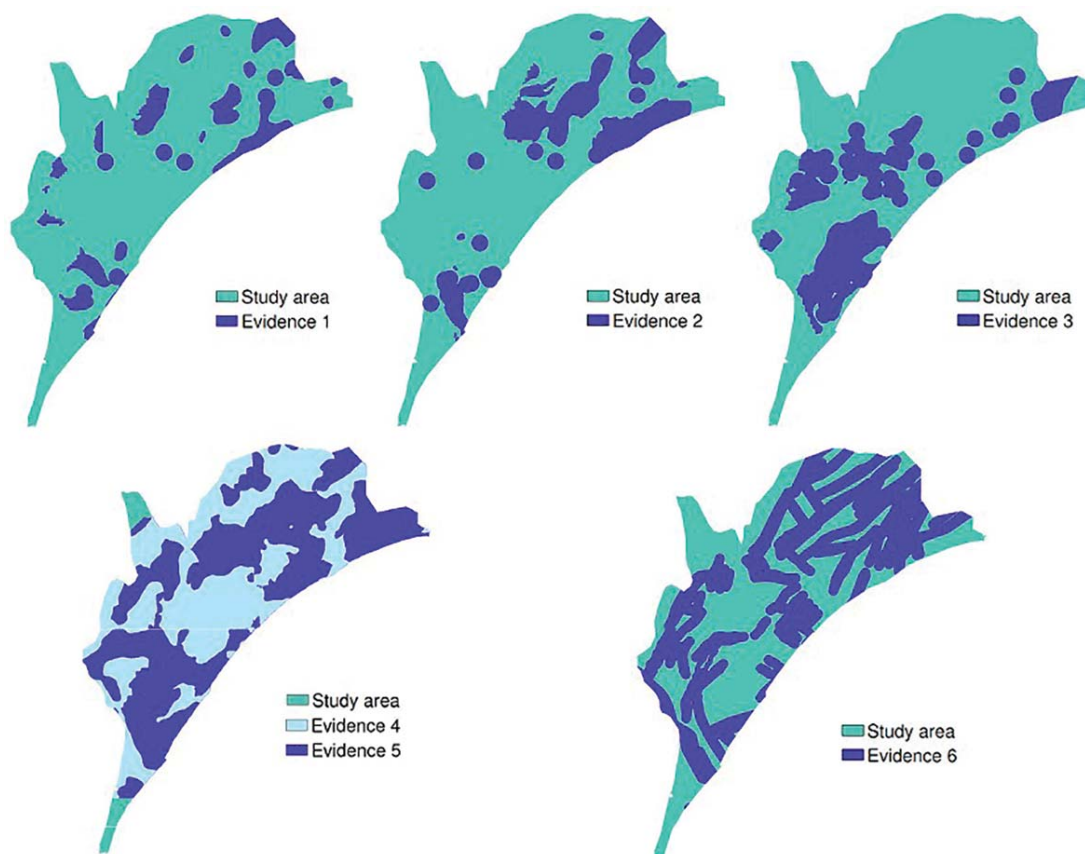


Figure 7 – Basement faults interpreted from seismic lines and crystalline basement upper part relief.

Table 1 – Exploratory evidences.

B_j	Evidence	Criteria	Area (km ²)	D
1	Pre-rift	Thickness >160 m	810.72	182
2	Indivisa rift	Thickness >160 m	1141.03	230
3	5th Rift	Thickness >160 m	1422.96	452
4	Positive Bouguer	mGal >0	2709.00	58
5	Negative Bouguer	mGal <0	2172.15	428
6	Basement faults	Buffer 1,500 m	2622.01	335

**Figure 8** – Exploratory evidences.

RESULTS

The results obtained by the applied methodology is presented here in two steps: calculus of the weights and generation of the *posteriori* favorability maps.

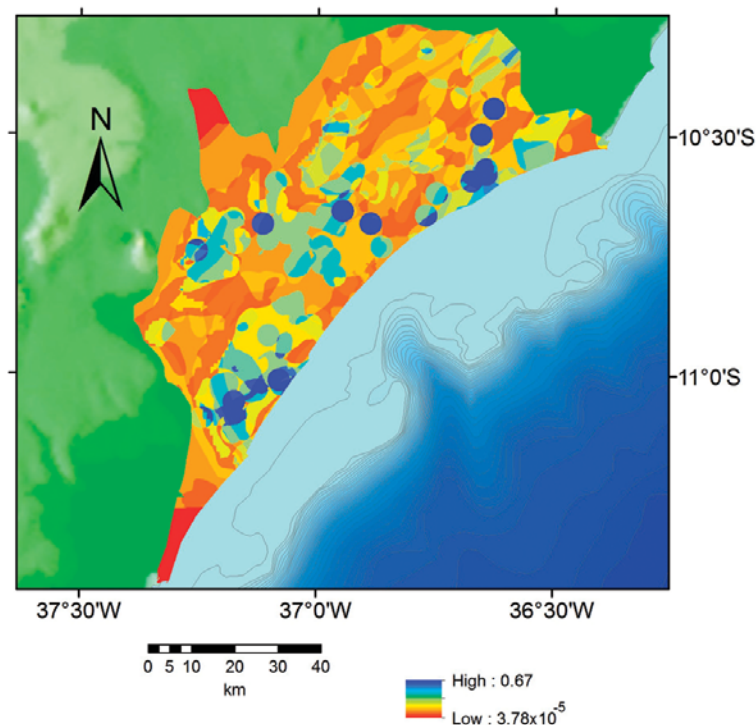
The calculi of the weights were carried out for each evidence with respect to the portion of the wells used for the favorability evaluation. The presented maps were produced by the sum of the *posteriori* probability log for each considered evidence, as presented by Equation (5), Section 2 (methodology). The study considered the evidences that showed $W+$ with a value over 1.20

(or $\log(W+) > 0.2$) in the proposition of the exploratory favorability map, so $B_j = 5$ was not considered. The obtained values by the probability *a posteriori* from considered B_j maps were summed and presented in color scale where blue color represents the most favorable result and red color represents the most unfavorable results.

To validate the proposed model, the evidences were evaluated with the 70% first discoveries (342 of 487 exploratory wells). The obtained weights for 70% first discoveries are shown in Table 2 and Figure 9.

Table 2 – Weights of evidences calculated for the exploratory evidence evaluation in Sergipe-Alagoas basin with 70%.

B_j	Evidence	$W+$	$Log(W+)$
1	Pre-rift	2.48	0.91
2	Indivisa rift	2.18	0.78
3	5th Rift	3.32	1.20
4	Positive Bouguer	1.92	0.65
5	Negative Bouguer	0.21	-1.55
6	Basement faults	1.31	0.27

**Figure 9** – Exploratory favorability map of Sergipe-Alagoas basin with 70% first discoveries.

The favorability areas presented in Figure 8 were compared to the remaining 145 exploratory wells with discoveries drilled (30%). The results presented in Figure 10 confirm the tendency of discoveries concentration in most favorable areas, standatized in 1-100 scale, where 100 represents the most favorable. In particular, note that 67% of discoveries are situated in the 64% superior level of favorability appointed by the model.

The results found using the WOFE model show that the proposed evidences are compliant with the data from the considered exploratory wells that present discoveries, and the methodology proved adequate. The final weights calculated for Sergipe-Alagoas basin, now considering 100% of data, are presented in Table 3 and Figure 10, respectively.

To clarify the application of the method, the values obtained by the model application are presented as follows. The study area of $t = 5,006.35 \text{ km}^2$ was discretized in $T = 500,635$ cells, which has $D = 487$ exploration wells drilled with discoveries. The prior probability that a randomly chosen cell presents a discovery in the study area results in $P(Oc) = \frac{D}{T} = 9.73 \cdot 10^{-5}$.

The evidence $J = 1$ (Pre-rift) was considered with area of 810.72 km^2 (discretized in $B_1 = 81,072$ cells) and $Oc = 182$ discovery cells. By applying the Equation (1) with respect to the probability of selecting a cell with the occurrence of reservoir given that evidence 1 is present, the value of $P(Oc/B_j) = \frac{P(B_j/Oc)P(Oc)}{P(B_j)} = 0.37$. In a similar way, Equation (2) allows us to calculate the probability of not finding a reservoir given that

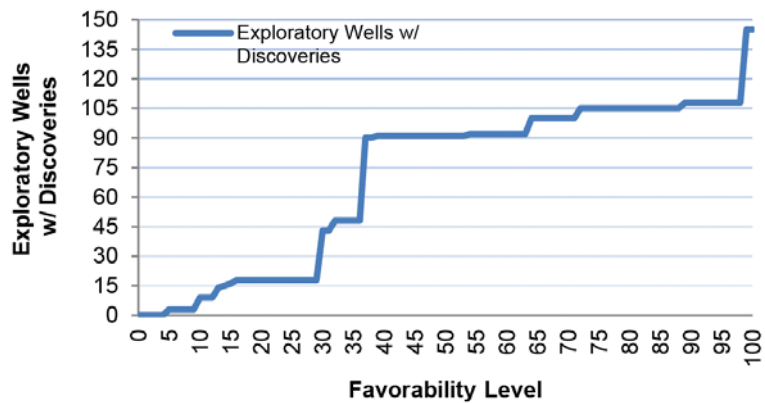


Figure 10 – Evaluation of exploratory map with 70% first discoveries.

Table 3 – Weights of evidences for Sergipe-Alagoas basin.

B_j	Evidence	$W+$	$Log(W+)$
1	Pre-rift	2.31	0.83
2	Indivisa rift	2.08	0.73
3	5th Rift	3.28	1.18
4	Positive Bouguer	2.03	0.71
5	Negative Bouguer	0.22	-1.51
6	Basement faults	1.31	0.27

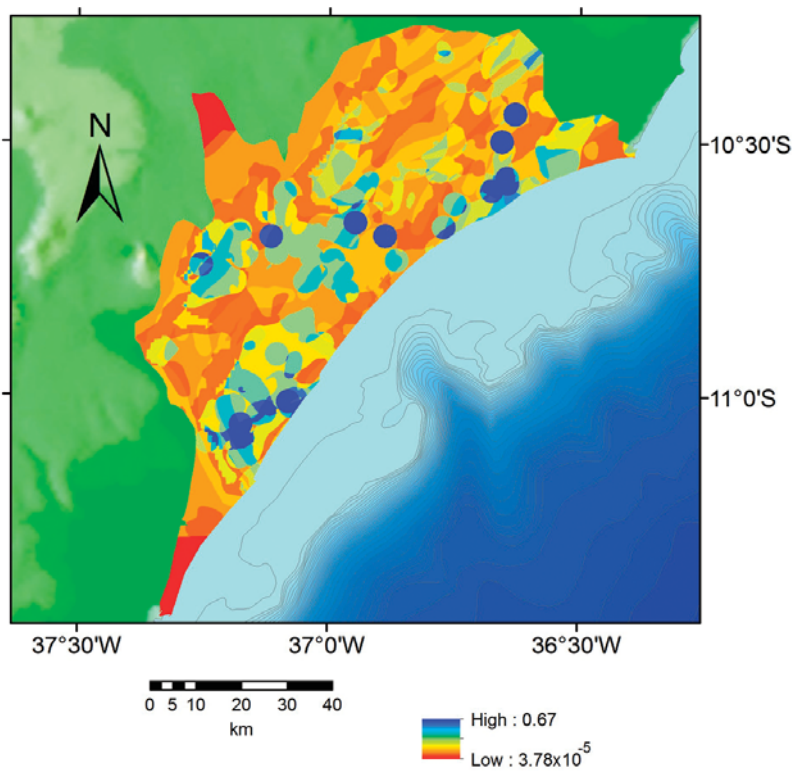


Figure 11 – Exploratory favorability map of Sergipe-Alagoas basin.

evidence 1 is present is

$$P(Oc/\overline{B_j}) = \frac{P(\overline{B_j}/Oc)P(Oc)}{P(\overline{B_j})} = 0.16.$$

The weighted value for evidence 1 is $W_j^+ = \frac{P(B_j/Oc)}{P(B_j/Oc)} = 2.31$ and its natural log is 0.83.

The favorability map sums the log value of the weight evidences calculated in the regions where they are present, together the value $\log(O(Oc)) = \frac{D}{T-D} = \frac{P(Oc)}{P(1-Oc)} = 9.74 \cdot 10^{-5}$ in accordance with Equation (5).

CONCLUSION

We proposed the favorability evaluation of hydrocarbon evidences by means of the Weights of Evidence approach and applied this approach to the Sergipe-Alagoas basin for validation. Such a model allows one to evaluate the favorability of areas of interest in a consistent, easily updatable way. The output of the model can be used as a tool for the decision-making process concerning the exploratory activities.

To validate the approach, we firstly applied it to 70% of the exploratory wells in the Sergipe-Alagoas basin, to obtain a model and confront the output of this model with the 30% remaining data. The validation confirmed the tendency of discoveries to be concentrated in the most favorable areas of the favorability map. The complete output, a favorability map organizing the area of interest into different favorability levels, can help the decision-maker identify target areas for further exploration, data gathering or area relinquishment.

It is worth mentioning that the model can be easily updated with new, relevant exploratory information, especially providing from newly drilled wells. The new output can then be used to update the favorability maps, with views to reinforcing previous assessments or dismissing them, whenever necessary. We argue that proposed methodology decreases the exposure of investments to the quantified uncertainties, causing impacts on the success of the E&P activities based on its historic results, as demonstrated in the case study of the Sergipe-Alagoas basin.

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